

DEPARTMENT OF MATHEMATICS				CLASS: II B.Sc. Mathematics				
Sem	Course Type	Course Code	Course Title	Credits	Contact Hours/week	CIA	Ext	Total
III	Major	20U3MMC5	Graph Theory	3	4	25	75	100

Nature of Course			
Knowledge and skill			Employability oriented
Skill oriented	✓		Entrepreneurship oriented

### Objectives:

Graph Theory is one of the most flourishing branches of Mathematics with wide applicability in a variety of areas ranging from Engineering to Molecular Biology. The objective of this course is to introduce basic concepts in the theory of graphs and to develop problem-solving ability and mathematical maturity in this area.

### Course content:

Unit	Description	Hours	K-Level	CLO(s)
I	<b>BASICS:</b> Graphs – Pictorial representation – Subgroups – Isomorphism and degrees – Walks and connected graphs – Cycles in graphs – Cut-vertices and cut-edges.	9	K3	1
II	<b>EULERIAN AND HAMILTONIAN GRAPHS:</b> Eulerian graphs – Fleury’s algorithm –Hamiltonian graphs – weighted graphs.	9	K4	2
III	<b>BIPARTITE GRAPHS AND MATRICES:</b> Bipartite graphs – Marriage problem – Trees –Connector problem – Matrix representations – Vector spaces associated with graphs – Cycle space – cut-set space.	9	K3	3
IV	<b>PLANAR GRAPHS:</b> Planar Graphs – Euler formula – Platonic solids – Dual of a plane graph – Characterization of planar graphs.	9	K3	4
V	<b>GRAPH COLOURINGS:</b> Vertex colouring – Edge colourings – An algorithm for vertex colouring.	9	K3	5

### **Book or study:**

- S.A.Choudum– A First Course in Graph Theory, Macmillan India Limited, 1987.  
UNIT I – 1.1 to 1.7  
UNIT II – 2.1 to 2.4  
UNIT III – 3.1 to 3.4 and 4.1 to 4.4  
UNIT IV – 5.1 to 5.5  
UNIT V – 6.1 to 6.3

### **Books for Reference:**

1. S. Arumugam and S. Ramachandran, - *Invitation to Graph Theory*, SCITECH publications (India) Pvt. Ltd, Chennai, 2006.
2. Gary Chartrand and Ping Zhang. *Introduction to Graph Theory*. New Delhi; New York : Tata McGraw-Hill Pub. Co. 2006.
3. Robin J.Wilson, *Introduction to Graph Theory*, Pearson publications, 5<sup>th</sup> Edition, 2010.

### **Web Resources**

- <https://d3gt.com>
- [https://www.brianheinold.net/graph\\_theory/graph\\_theory\\_book.html](https://www.brianheinold.net/graph_theory/graph_theory_book.html)
- [https://www.youtube.com/playlist?list=PLoJC20gNfC2gmT\\_5WgwYwGMvgCjYVsIQg](https://www.youtube.com/playlist?list=PLoJC20gNfC2gmT_5WgwYwGMvgCjYVsIQg)

### **Rationale for Nature of the course:**

This course namely Graph Theory has applications in various fields. Graph theory has been serving as an elegant tool to easily approach/solve several problems/concepts in other fields ranging from Science to Sociology. This course will enable the students to acquire skills by which they can model certain real-life problems as graph theoretical terms and can make inference.

### **Activities having direct bearing on Skill development / Employability / Entrepreneurship:**

Modeling certain real-life problems like Scheduling problem, Traffic signal problem, Marriage problem and so on.

**Pedagogy:** Chalk and Talk, PPT, Group Discussion, Quiz, Seminar, Problem solving, Tutorial, LMS (CANVAS, FLICKERS).

## Course Learning Outcomes

On the successful completion of the course, students will be able to

CLO #	Description	K -Level
CLO1	Identify various types of sub graphs of a graph, to find degree sequence of a graph, to identify isomorphic graphs, to determine connectedness of a graph, to list out cut-vertices and cut-edges of the given graph	Up to K3
CL02	Determine whether graphs are Hamiltonian and/or Eulerian	Up to K4
CL03	Recognize bipartite graphs, to find various matrices representing a graph, to determine vector spaces associated with a given graph and also to solve problems involving Matchings and trees	Up toK3
CL04	Identify planar graphs, to find dual of a plane graph	Up to K3
CL05	Find minimum vertex and edge coloring of certain families of graphs	Up to K3

K1- Remembering and recalling facts with specific answers

K2- Basic understanding of facts and stating main ideas with general answers

K3- Application oriented- Solving Problems

K4- Examining, analyzing, presentation and make inferences with evidences

## Mapping with Programme Specific Outcome

	PSO1	PSO2	PSO3	PSO4	PSO5	PSO6	PSO7
CLO1	3	1	1				2
CLO2	3	1				1	
CLO3	3	2	1		1	2	1
CLO4	3		2	1	1	2	
CLO5	3	2	2		1	2	1

## Mapping with Programme Outcome

	PO1	PO2	PO3	PO4	PO5
CLO1	3				
CLO2	2		2		
CLO3	2	1	3		
CLO4	2				
CLO5	1		2		1

1- Basic Level

2- Intermediate Level

3- Advanced Applications

**BLUE PRINT (for External Examinations)**  
**Articulation Mapping –K Levels with Course Learning Outcomes (CLOs)**

Sl.No	CLOs	K- Level	Section A		Section B		Section C (Either/or Choice)	Section D (Open Choice)
			MCQs		Short Answers			
			No. of Questions	K- Level	No. of Questions	K- Level		
1	CLO 1	Up to K3	2	K1/ K2	1	K1	2 (K2/K2)	1(K3)
2	CLO 2	Up to K4	2	K1/ K2	1	K1	2 (K4/K4)	1(K4)
3	CLO 3	Up to K3	2	K1/ K2	1	K2	2 (K3/ K3)	1(K3)
4	CLO 4	Up to K3	2	K1/ K2	1	K2	2 (K3 /K3)	1(K2)
5	CLO 5	Up to K3	2	K1/ K2	1	K2	2 (K1/ K1)	1(K3)
No. of Questions to be asked			10		5		10	5
No. of Questions to be answered			10		5		5	3
Marks for each question			1		2		5	10
Total Marks for each section			10		10		25	30

K1- Remembering and recalling facts with specific answers

K2- Basic understanding of facts and stating main ideas with general answers

K3- Application oriented- Solving Problems

K4- Examining, analyzing, presentation and make inferences with evidences

**Distribution of Section-wise Marks with K levels**

K Levels	Section A (No choice)	Section B (No choice)	Section C (Either/ or)	Section D (Open choice)	Total marks	% of marks without choice	Consoli- dated
K1	5	4	10	-	19	15.83	41.66%
K2	5	6	10	10	31	25.83	
K3	-	-	20	30	50	41.67	41.67
K4	-	-	10	10	20	16.67	16.67
Total marks	10	10	50	50	120	100	100%

**Blue Print for CIA - I**  
**Articulation Mapping –K Levels with Course Learning Outcomes (CLOs)**

Sl.No	CLOs	K- Level	Section A		Section B		Section C (Either/or Choice)	Section D (Open Choice)
			MCQs		Short Answers			
			No. of Questions	K- Level	No. of Questions	K- Level		
1	CLO 1	Up to K3	2	K1/ K2	1	K2/K2	2 (K2/K2)	1(K3)
2	CLO 2	Up to K4	2	K1/ K2	2	K1	2 (K3/K3)	1(K3) 1(K4)
No. of Questions to be asked			4		3		4	3
No. of Questions to be answered			4		3		2	2
Marks for each question			1		2		5	10
Total Marks for each section			4		6		10	20

K1- Remembering and recalling facts with specific answers

K2- Basic understanding of facts and stating main ideas with general answers

K3- Application oriented- Solving Problems

K4- Examining, analyzing, presentation and make inferences with evidences

**Blue Print for CIA - II**  
**Articulation Mapping –K Levels with Course Learning Outcomes (CLOs)**

Sl.No	CLOs	K- Level	Section A		Section B		Section C (Either/or Choice)	Section D (Open Choice)
			MCQs		Short Answers			
			No. of Questions	K- Level	No. of Questions	K- Level		
1	CLO 3	Up to K3	2	K1/ K2	2	K1/ K2	2 (K2/K2)	2(K3)
2	CLO 4	Up to K3	2	K1/ K2	1	K2	2 (K3 /K3)	1(K3)
No. of Questions to be asked			4		3		4	3
No. of Questions to be answered			4		3		2	2
Marks for each question			1		2		5	10
Total Marks for each section			4		6		10	20

K1- Remembering and recalling facts with specific answers

K2- Basic understanding of facts and stating main ideas with general answers

K3- Application oriented- Solving Problems

K4- Examining, analyzing, presentation and make inferences with evidences

## COURSE PLAN

Unit	Description	Hours	Pedagogy
I	Graphs – Pictorial representation	1	Chalk and talk, D3 Graph Theory – ICT tool, Interaction, Group Discussion
	Subgroups	1	
	Degrees	1	
	Isomorphism	1	
	Walks and connected graphs	2	
	Cycles in graphs	1	
	Cut-vertices and cut-edges	1	
	Tutorial	1	
II	Introduction to Eulerian graphs	1	Chalk and talk, PPT, D3 Graph Theory – ICT tool, Interaction, Group Discussion and e - quiz
	Theorems on Eulerian graphs	2	
	Fleury’s algorithm to find Eulerian trail	1	
	Hamiltonian graphs	2	
	weighted graphs	2	
	Tutorial	1	
III	Bipartite graphs	1	Chalk and talk, PPT, D3 Graph Theory – ICT tool, Interaction, Assignment and Seminar
	Marriage problem	1	
	Trees	2	
	Connector problem	1	
	Matrix representations	1	
	Vector spaces associated with graphs Cycle space – cut-set space.	2	
	Tutorial	1	
IV	Introduction to Planar Graphs – definition and example	1	Chalk and talk, PPT, D3 Graph Theory – ICT tool, Interaction and e-Quiz
	Properties of planar graphs	2	
	Euler formula for plane graphs and its	1	
	Platonic solids	1	
	Dual of a plane graph	1	
	Characterization of planar graphs	2	
	Tutorial	1	
V	Vertex colouring – definition and examples	1	Chalk and talk, D3 Graph Theory – ICT tool, Assignment and Interaction
	Theorems on vertex colouring	2	
	Algorithm to find a minimum vertex colouring	1	
	Introduction to Edge colouring	1	
	Results on edge colouring	3	
	Tutorial	1	

### Course Designer :

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